

# RAMAKRISHNA MISSION VIDYAMANDIRA

Belur Math, Howrah - 711202

B. Sc ADMISSION TEST - 2025

MATHEMATICS

Date : 23/06/2025

Full marks : 100

Time : 12:30 pm – 2:30 pm

**SET: A**

## Instructions for the candidates

- Answer all questions.
- Each question has 4 options out of which only one is correct.
- Tick (✓) the correct option on Answer Sheet.
- The tick (✓) must be very clear – if it is smudgy or not clear, no marks will be awarded.
- Each correct answer carries **2 marks** and for each incorrect answer **1 mark** will be deducted.
- Unanswered questions will not be awarded.
- Multiple answers will be considered as wrong answer.
- Calculator, smartwatch are **not** allowed.

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1. If the lines  $x + 2ay + a = 0$ ,  $x + 3by + b = 0$  and  $x + 4cy + c = 0$  are concurrent then  $a, b, c$  are  
(a) in AP                      (b) in GP                      (c) in HP                      (d) None of (a), (b) and (c)
  2. If the point  $(3, 4)$  lies inside and the point  $(-3, -4)$  lies outside the circle  $x^2 + y^2 - 7x + 5y - p = 0$ , then the set of all possible values of  $p$  is  
(a)  $(23, 25)$                       (b)  $(24, 26)$                       (c)  $(24, 25)$                       (d)  $(0, 25)$
  3. An equilateral triangle is inscribed in the parabola  $y^2 = 4x$ , one of whose vertex is at vertex of the parabola, the length of each side of the triangle is  
(a)  $8\sqrt{3}$                       (b)  $4\sqrt{3}$                       (c)  $\frac{\sqrt{3}}{2}$                       (d)  $\sqrt{\frac{3}{2}}$
  4. The reflection point of the point  $(0, 3, -2)$  in the line  $\frac{1-x}{2} = 2 - y = 1 + z$  is  
(a)  $(2, 1, 0)$                       (b)  $(2, 1, 4)$                       (c)  $(1, 2, -1)$                       (d)  $(0, 0, 1)$
  5. The equation of a plane passing through the line of intersection of the planes  $x + 2y + 3z = 2$  and  $x - y + z = 3$  and at a distance  $\frac{2}{\sqrt{3}}$  from the point  $(3, 1, -1)$  is  
(a)  $5x - 11y + z = 17$                       (b)  $x + y + z = \sqrt{3}$   
(c)  $\sqrt{2}x + y = \sqrt{3}z - 1$                       (d)  $x + \sqrt{2}y = 1 - \sqrt{2}z$
  6. If  $y = x$  and  $3y + 2x = 0$  are the equations of a pair of conjugate diameters of an ellipse, then the eccentricity of the ellipse is  
(a)  $2\sqrt{3}$                       (b)  $\frac{1}{\sqrt{3}}$                       (c)  $\frac{1}{3}$                       (d)  $\frac{1}{\sqrt{2}}$

7. The nonzero vectors  $\vec{a}, \vec{b}$  and  $\vec{c}$  are related as  $\vec{b} = 5\vec{a}$  and  $\vec{c} = -2\vec{b}$ . The angle between  $\vec{a}$  and  $\vec{c}$  is  
 (a)  $\frac{\pi}{2}$  (b)  $\frac{\pi}{3}$  (c)  $\frac{\pi}{4}$  (d)  $\pi$
8. Let  $f(x) = \begin{cases} 1 + \frac{x^3 + x^2 - 16x + 20}{(x-2)^2}, & x \neq 2 \\ p, & x = 2. \end{cases}$   
 If  $f(x)$  is continuous for all  $x \in \mathbb{R}$ , then  $p$  equals  
 (a) 8 (b)  $\pm 8$  (c)  $\frac{1}{8}$  (d)  $-8$ .
9.  $\lim_{x \rightarrow 0} \frac{\sin(\pi \cos^2 x)}{2x^2}$  is equal to  
 (a)  $\frac{\pi}{2}$  (b) 2 (c)  $-\pi$  (d)  $\pi$ .
10. For  $x \in \mathbb{R}$ ,  $f(x) = |\log 3 - \sin x|$  and  $g(x) = f(f(x))$ . Then  $g'(0)$  equals  
 (a)  $\log 3$  (b)  $\sin(\log 3)$  (c)  $\cos(\log 3)$  (d)  $-\sin(\log 3)$ .
11. Let  $f(x) = \begin{cases} e^{\frac{1}{x}}, & x \neq 0 \\ 0, & x = 0. \end{cases}$   
 Then  
 (a)  $f(x)$  is discontinuous at  $x = 0$ .  
 (b)  $\lim_{x \rightarrow 0^+} f(x) = 0$   
 (c)  $\lim_{x \rightarrow 0^-} f(x) = 1$   
 (d)  $\lim_{x \rightarrow 0^+} f(x) = e$
12. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a positive increasing function with  $\lim_{x \rightarrow \infty} \frac{f(4x)}{f(x)} = 1$ . Then  $\lim_{x \rightarrow \infty} \frac{f(3x)}{f(x)}$  is equal to  
 (a)  $\frac{1}{2}$  (b)  $\frac{3}{4}$  (c)  $\frac{4}{3}$  (d) 1.
13.  $\lim_{x \rightarrow 2} \frac{3^x + 3^{3-x} - 12}{3^{-x/2} - 3^{1-x}}$  is equal to  
 (a) 36 (b) 3 (c) 1 (d)  $-12$ .
14. The set of points of continuity of the function  $f(x) = \begin{cases} \frac{x}{|x|}, & x < 0 \\ -1, & x \geq 0 \end{cases}$  is  
 (a)  $\mathbb{R}$  (b)  $\mathbb{R} \setminus \{0\}$  (c)  $\{0\}$  (d)  $\mathbb{R} \setminus \{1, -1\}$ .
15. If  $A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$  and  $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$  satisfy  $A^2 = 8A + kI$ , then  $k$  is  
 (a) 6 (b) 7 (c)  $-6$  (d)  $-7$
16. For  $x, y > 0$ ,  $\begin{vmatrix} \log_x y & 1 \\ 1 & \log_y x \end{vmatrix} =$   
 (a) 2 (b) 1 (c)  $-1$  (d) 0

17. If  $3^x + 2^y = 7$  and  $4^y - 9^x = 7$ , then  
 (a)  $x = 1, y = 2$       (b)  $x = 2, y = 1$       (c)  $x = 1, y = 3$       (d)  $x = 3, y = 2$
18. The 7th term in the expansion of  $(3x + \frac{2}{x})^{11}$  is  
 (a)  $3849120x^3$       (b)  $10777536x$       (c)  $\frac{7185024}{x}$       (d)  $\frac{3421440}{x^3}$
19. The sum of the numbers divisible by 13 between 500 and 1000 is  
 (a) 28305      (b) 28405      (c) 27417      (d) 28505
20. Sum of the first 20 terms of the series  $\frac{1^3}{1} + \frac{1^3+2^3}{1+3} + \frac{1^3+2^3+3^3}{1+3+5} + \dots$  is  
 (a) 829.5      (b) 839.5      (c) 827.5      (d) 827.75
21. The smallest n, for which the sum of the first n terms of the series  $1 + 3 + 3^2 + \dots$  is greater than 7000, is  
 (a) 10      (b) 9      (c) 11      (d) 8
22. If A, B are two sets and  $A \times B$  contains 7 elements, then  
 (a) Both A and B contain more than 1 element.  
 (b) One of the sets A, B contains 3 elements and the other contains 4 elements.  
 (c) One of the sets A, B contains 1 element and the other contains 7 elements.  
 (d) Both A, B contain less than 7 elements.
23. If a set A contains 5 elements and B contains 3 elements and if B is not a subset of A then the number of elements in  $A \cup B$  is  
 (a)  $\geq 7$       (b)  $\geq 6$       (c) = 8      (d) = 6
24. A relation  $\rho$  on the set  $\mathbb{Z}$  of all integers is defined by ' $a \rho b$  iff  $ab \geq 0$ ' ( $a, b \in \mathbb{Z}$ ). Then  
 (a)  $\rho$  is not reflexive      (b)  $\rho$  is not symmetric  
 (c)  $\rho$  is not transitive      (d)  $\rho$  is an equivalence relation.
25. A relation  $\rho$  on the set  $\mathbb{N}$  of all positive integers is defined by ' $a \rho b$  iff  $a^2 + b^2$  is even' ( $a, b \in \mathbb{N}$ ). Then  
 (a)  $\rho$  is not reflexive      (b)  $\rho$  is not symmetric  
 (c)  $\rho$  is not transitive      (d)  $\rho$  is an equivalence relation.
26. If n is the total number of maps from A to B where A has 2 elements and B has 4 elements, then  
 (a)  $n = 8$       (b)  $n = 12$       (c)  $n = 16$       (d)  $n = 20$
27. If n is the total number of surjective maps from A to B where A has 3 elements and B has 2 elements then  
 (a)  $n = 6$       (b)  $n = 4$       (c)  $n = 8$       (d)  $n = 9$

28. Suppose  $\mathbb{N}$  is the set of all positive integers and  $A = \{1, 2, 3\}$ . Then
- No map from  $\mathbb{N}$  to  $\mathbb{N} \setminus A$  is injective.
  - No map from  $\mathbb{N}$  to  $\mathbb{N} \setminus A$  is bijective.
  - there are only three bijective maps from  $\mathbb{N}$  to  $\mathbb{N} \setminus A$ .
  - there are more than three bijective maps from  $\mathbb{N}$  to  $\mathbb{N} \setminus A$ .
29. Let  $z_1$  and  $z_2$  be two complex numbers. Which of the following statement is false for  $z_1$  and  $z_2$ ?
- $z_1 + z_2 \leq \bar{z}_1 + \bar{z}_2$ .
  - $|z_1 + z_2| \leq |z_1| + |z_2|$ .
  - $|z_1 - z_2| \leq |z_1| + |z_2|$ .
  - $\overline{z_1 + z_2} = \bar{z}_1 + \bar{z}_2$ .
30. If a fourth degree polynomial  $P(x)$  can be written as  $(a_1x^2 + b_1x + c_1)(a_2x^2 + b_2x + c_2)$  and  $P(x) = 0$  has only non-real complex roots then which of the following statements is definitely true?
- $(b_1^2 - 4a_1c_1)(b_2^2 - 4a_2c_2) \geq 0$ .
  - $(b_1^2 - 4a_1c_1) + (b_2^2 - 4a_2c_2) \geq 0$ .
  - $(b_1^2 - 4a_1c_1) \geq 0, (b_2^2 - 4a_2c_2) \leq 0$ .
  - $(b_1^2 - 4a_1c_1) < 0, (b_2^2 - 4a_2c_2) < 0$ .
31. The modulus of  $\frac{7+i}{12+5i}$  is
- $\frac{\sqrt{50}}{13}$
  - $\frac{50}{13}$
  - $\sqrt{\frac{48}{119}}$
  - $\frac{8}{17}$ .
32. If  $x \sin^3 \theta + y \cos^3 \theta = \sin \theta \cos \theta$  ;  $x \sin \theta - y \cos \theta = 0$  and  $\sin \theta \cos \theta \neq 0$ , then which of the following statement is true?
- $x^2 - y^2 = 1$
  - $x^2 + y^2 = 1$
  - $x^3 + y^3 = 1$
  - $x^3 - y^3 = 1$ .
33. If  $n$  is a non-zero integer and  $\alpha$  is a real number, then  $\sin[n\pi + (-1)^n \alpha]$  is equal to
- $\sin \alpha$
  - $-\sin \alpha$
  - $\frac{n}{|n|} \sin \alpha$
  - $(-1)^n \sin \alpha$ .
34. Let  $z_1, z_2$  be two complex numbers such that  $|z_1 + z_2| = |z_1 - z_2|$ , then which of the following statement is definitely true?
- $z_1 = z_2$ .
  - $z_2 = 0$ .
  - Either  $Re(z_1)Re(z_2) = 0$  or  $Im(z_1)Im(z_2) = 0$ .
  - $Re(z_1)Re(z_2) + Im(z_1)Im(z_2) = 0$ .
- (Here,  $Re(z)$  and  $Im(z)$  stands for real and imaginary parts respectively.)
35. From a certain point P on the ground, the angle of elevation of the top of the tree is  $\alpha$ . After moving  $x$  meters towards the tree the angle of elevation becomes  $\beta$ . Then, the height  $h$  of the tower is given by
- $h = \frac{x \tan \alpha \tan \beta}{\tan \beta + \tan \alpha}$
  - $h = \frac{x \tan \alpha \tan \beta}{\tan \beta - \tan \alpha}$
  - $h = \frac{\tan \alpha \tan \beta}{x(\tan \beta \tan \alpha)}$
  - $h = \frac{-\tan \alpha \tan \beta}{x(\tan \beta + \tan \alpha)}$

36. A particle moves along a straight line and its distance  $x$  from a fixed point on the line at time  $t$  is given by  $t = Ax^2 + Bx + C$ , where  $A, B, C$  are positive constants. If  $v$  is the velocity of the particle at time  $t$ , then the particle is moving with retardation  
 (a)  $Av^2$  (b)  $2Av^2$  (c)  $Av^3$  (d)  $2Av^3$
37. The area ( in square unit ) bounded by the parabola  $y = x^2 - 6x + 10$  and the straight lines  $x = 6$  and  $y = 2$  is  
 (a)  $\frac{16}{3}$  (b)  $\frac{20}{3}$  (c) 8 (d)  $\frac{32}{3}$
38. The angle between the curves  $y = \sin x$  and  $y = \cos x$  is  
 (a)  $\tan^{-1}(5\sqrt{2})$  (b)  $\tan^{-1}(2\sqrt{2})$  (c)  $\tan^{-1}(3\sqrt{2})$  (d)  $\tan^{-1}(3\sqrt{3})$
39. A land in the form of a circular sector has been fenced by wire 40 metre length. The area of the land will be maximum when the radius of the circular sector ( in metre ) is  
 (a) 25 (b) 20 (c) 10 (d) 15
40. A stone falling from the top of a vertical tower has descended  $x$  feet when another is let fall from a point  $y$  feet below the top. If they fall from rest and reach the ground together, then the height of the tower in feet is  
 (a)  $\frac{(x+y)^2}{2x}$  (b)  $\frac{(x+y)^2}{2y}$  (c)  $\frac{(x+y)^2}{4x}$  (d)  $\frac{(x+y)^2}{4y}$
41. Value of  $\int_1^2 [x^2] dx$  is (where  $[x]$  is the greatest integer function of  $x$ )  
 (a)  $5 + \sqrt{3} - \sqrt{2}$  (b)  $5 - \sqrt{3} + \sqrt{2}$  (c)  $5 - \sqrt{3} - \sqrt{2}$  (d)  $5 + \sqrt{3} + \sqrt{2}$
42. The minimum value of  $f(x) = |3-x| + |2+x| + |5-x|$  is  
 (a) 0 (b) 8 (c) 7 (d) 10
43. Two numbers  $a$  and  $b$  are chosen at random from the set of first 30 natural numbers. The probability that  $(a^2 - b^2)$  is divisible by 3 is  
 (a)  $\frac{47}{87}$  (b)  $\frac{44}{87}$  (c)  $\frac{46}{87}$  (d)  $\frac{15}{29}$
44. Among all possible arrangements of the letters of the word **NUMBER**, where the position of each of the vowels remains unchanged, the dictionary order of 'NUMBER' is  
 (a) 16 (b) 15 (c) 14 (d) 13.
45. The number of integral solutions of  $x + y + z = 0$  with  $x, y, z \geq -4$  is  
 (a) less than 90 (b) 90 (c) 91 (d) more than 91.
46. The number of four-digit odd numbers that contain 1 exactly once is  
 (a) 648 (b) 324 (c) 2916 (d) 1548
47. Let  $ABC$  be a triangle and we fix 3, 4 and 5 points on the sides  $AB, BC$  and  $CA$ , respectively. The number of triangles that can be formed using these points is  
 (a) 60 (b) 205 (c) 220 (d) 105

48. If  $P(A) = P(B) = P(C) = 0.6$  and  $P(A \cap B) = P(B \cap C) = P(C \cap A) = 0.3$ , then
- (a)  $P(A \cap B \cap C) \leq 0.1$                       (b)  $P(A \cap B \cap C) = 0.15$   
(c)  $P(A \cap B \cap C) < 0.1$                       (d)  $P(A \cap B \cap C) > 0.$
49. In an experiment of rolling an unbiased die twice, the probability that sum of the faces is divisible by 3, is
- (a)  $\frac{1}{3}$                                               (b)  $\frac{1}{2}$                                               (c)  $\frac{1}{6}$                                               (d)  $\frac{1}{4}$ .
50. From an urn containing 5 distinguishable black balls and 6 distinguishable white balls, two balls are selected at random. The probability that the selected balls are of different colour, is
- (a)  $\frac{2}{11}$                                               (b)  $\frac{5}{11}$                                               (c)  $\frac{6}{11}$                                               (d)  $\frac{1}{11}$ .

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